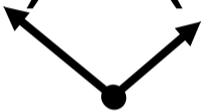


Rules for Multiplication & Division

$$(-) \times (-) = (+)$$


$$(+) \times (+) = (+)$$


Both signs the same
then the answer is (+)

$$(-) \div (-) = (+)$$

$$(+) \div (+) = (+)$$

$$(-) \times (+) = (-)$$

$$(+) \times (-) = (-)$$


Signs different then
the answer is (-)

$$(-) \div (+) = (-)$$

$$(+) \div (-) = (-)$$

You Try

1) Use rules

a) $(-7)(-11)$
 $(+77)$

b) $(-56) \div (-2)$
 $(+28)$

c) $(+14) \times (-2)$
 (-28)

d) $(+24) \div (-4)$
 (-6)

2) Find the product using the distributive property ^{box method}

$$(-97) \times (-31) = (+3007)$$

| | | |
|----|-----------------------|---------------------|
| | 90 | 7 |
| 30 | $90 \times 30 = 2700$ | $7 \times 30 = 210$ |
| 1 | $1 \times 90 = 90$ | $1 \times 7 = 7$ |

$$\begin{array}{r} 2700 \\ 210 \\ + 90 \\ 7 \\ \hline 3007 \end{array}$$

3) Circle all the incorrect statements below and make corrections

$(-35) \div 7 = 5$
↓
 -5

$(-12) \times (-3) = (36)$

$(-20) \times (+2) = (-10)$
↓
 -40

$(24) = (-8)$
 -3

$(4)(-11) = (44)$
↓
 -44

$(-6) \times (+7) = (-42)$

Two types of Probability

Theoretical Probability - is what is expected to happen based on theory of math. Use a formula. (Today we are doing this)

$$P(\text{event}) = \frac{\text{\# of favorable outcomes}}{\text{Total \# of possible outcomes}}$$

Ex) $P(\text{head on coin}) = \frac{\text{\# of heads}}{\text{Total sides of coin}} = \frac{1}{2}$



↙
Must write out Probability Statements for questions

Experimental Probability - is found by repeating an experiment and observing the outcomes. (Doing it out....not today)

$$P(\text{event}) = \frac{\text{number of times event occurs}}{\text{total number of trials}}$$

Example:

A coin is tossed 10 times:
A head is recorded 7 times
and a tail 3 times.

$$P(\text{head}) = \frac{7}{10}$$

$$P(\text{tail}) = \frac{3}{10}$$

We will focus on Theoretical Probability unless they give you the experimental data.

In word problems some words that can be used to suggest an event is INDEPENDENT is:

Replace or returned

$$P(A \text{ and } B \text{ and } C \text{ and } D)$$

$$= P(A) \times P(B) \times P(C) \times P(D)$$

Your Turn

$$\begin{aligned} \text{Total} &= 5 + 3 + 2 + 10 \\ &= 20 \end{aligned}$$

Ex 3) A bag contains 5 orange marbles, 3 pink marbles, 2 green marbles and 10 Blue marbles



a) What is the probability of orange? (as fraction and percent)

$$P(\text{orange}) = \frac{\# \text{orange}}{\text{Total}} = \frac{5}{20} \xrightarrow{\text{Reduce}} \frac{1}{4} = 25\%$$

Handwritten notes: A blue arrow points from 5 to 1 with 'x 1/5' written below it. A red arrow points from 20 to 4 with 'x 5' written below it. A red arrow points from 1/4 to 25/100 with 'x 25' written above it.

b) What is the probability of pink? (as fraction and percent)

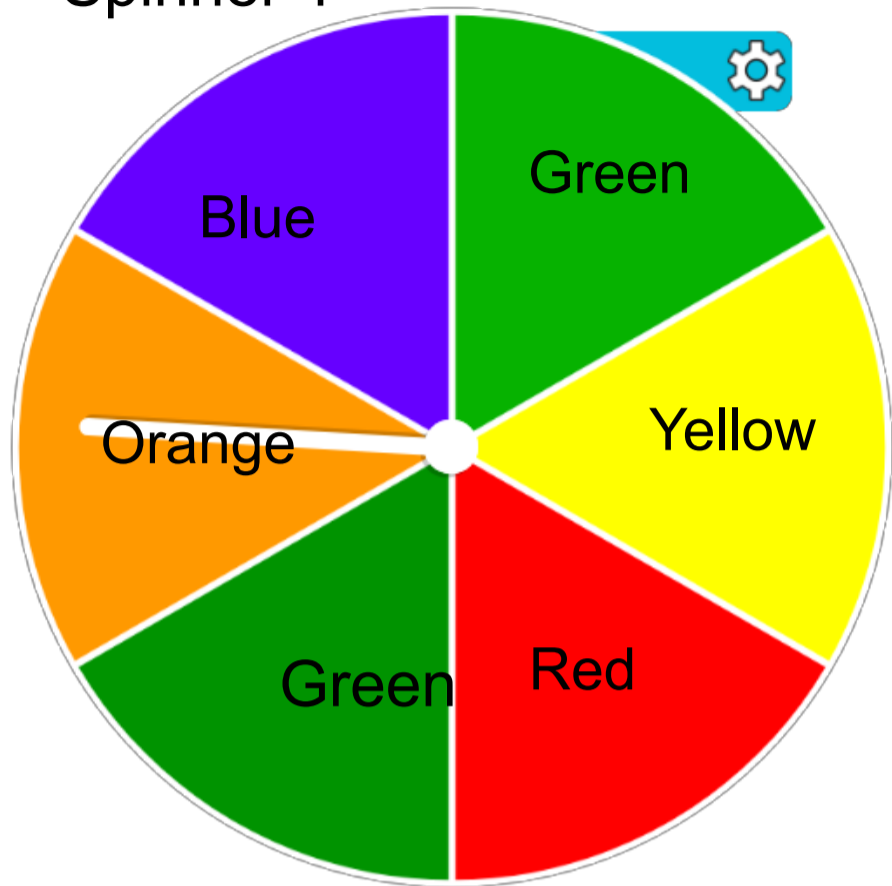
$$P(\text{pink}) = \frac{\# \text{pink}}{\text{Total}} = \frac{3}{20} \xrightarrow{\times 5} \frac{15}{100} = 15\%$$

Handwritten notes: A red arrow points from 3 to 15 with 'x 5' written above it. A red arrow points from 20 to 100 with 'x 5' written below it.

c) What is the probability of picking 3 marbles and all three are green?

$$\begin{aligned} P(3 \text{ Green}) &= P(\text{Green}) \times P(\text{Green}) \times P(\text{Green}) \\ &= \frac{2}{20} \times \frac{2}{20} \times \frac{2}{20} \quad \text{Reduce} \\ &= \frac{1}{10} \times \frac{1}{10} \times \frac{1}{10} \\ &= \frac{1}{1000} \\ &= 0.001 \\ &= 0.1\% \end{aligned}$$

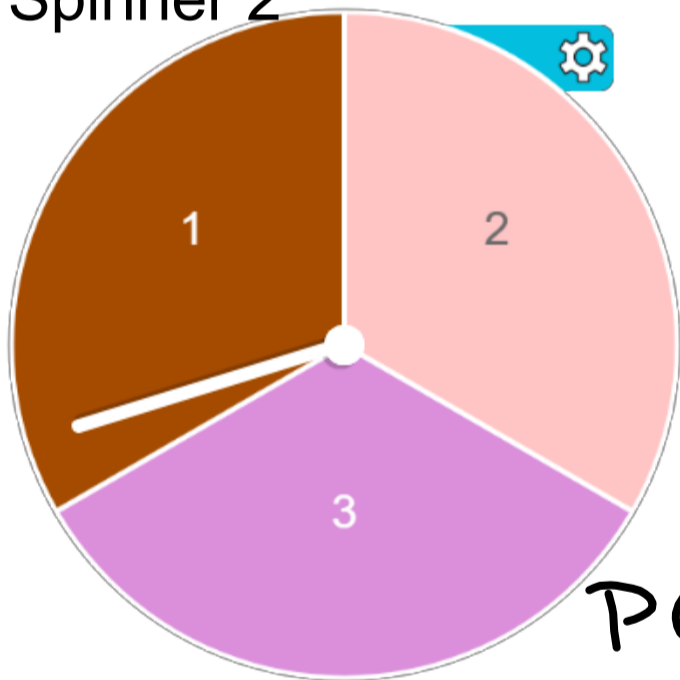
Spinner 1



1) What is the probability of spinning the spinner 1, twice and getting red and a green?

$$\begin{aligned} P(\text{Red and Green}) &= P(R) \times P(G) \\ &= \frac{1}{6} \times \frac{2}{6} \\ &= \frac{2}{36} \\ &= \frac{1}{18} \end{aligned}$$

Spinner 2



2) Petter spins the pointer on each spinner shown to the left at the same time. What is the theoretical probability of landing on yellow on the first spinner and 3 on the second spinner?

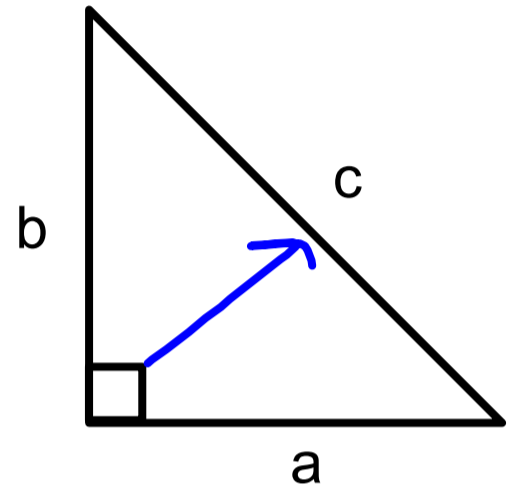
$$\begin{aligned} P(\text{Yellow And 3}) &= P(\text{Yellow}) \times P(3) \\ &= \frac{1}{6} \times \frac{1}{3} \\ &= \frac{1}{18} \end{aligned}$$

Pythagorean Theorem

- Right Angle Triangle has one angle that 90°
- the side directly across to the right angle is always the longest side, it is the **hypotenuse**.

We use "c" for the hypotenuse

- Legs are side "a" and "b"



Pythagorean Theorem Equation:

$$(a)^2 + (b)^2 = (c)^2$$

area of the square off
the hypotenuse

$$(c)^2 - (b)^2 = (a)^2$$

area of the square off
the leg

Pythagorean Triples:

Given 3 numbers

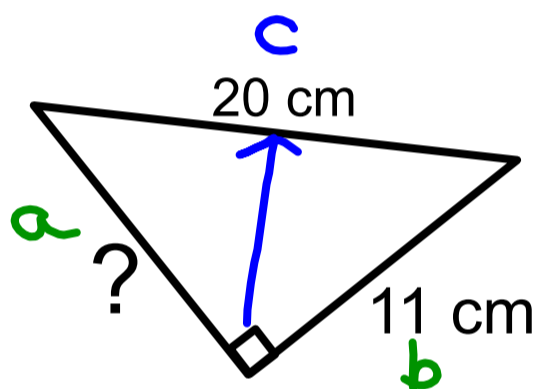
$$(c)^2 \left. \vphantom{(c)^2} \right\} (a)^2 + (b)^2$$



Find the length of the missing side

(Use calculators but show your work)

a)



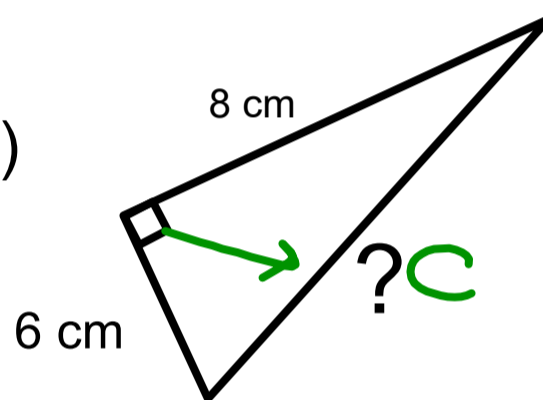
$$a^2 = c^2 - b^2$$
$$a^2 = (20\text{cm})^2 - (11\text{cm})^2$$
$$a^2 = 400\text{cm}^2 - 121\text{cm}^2$$

$$a^2 = 279\text{cm}^2$$

$$\sqrt{a^2} = \sqrt{279\text{cm}^2}$$

$$a = 16.7\text{cm}$$

b)



$$c^2 = a^2 + b^2$$
$$c^2 = (6\text{cm})^2 + (8\text{cm})^2$$
$$c^2 = 36\text{cm}^2 + 64\text{cm}^2$$

$$c^2 = 100\text{cm}^2$$

$$\sqrt{c^2} = \sqrt{100\text{cm}^2}$$

$$c = 10\text{cm}$$

Fill in the blanks

1) $(\underline{-9}) \times (-8) = (+72)$

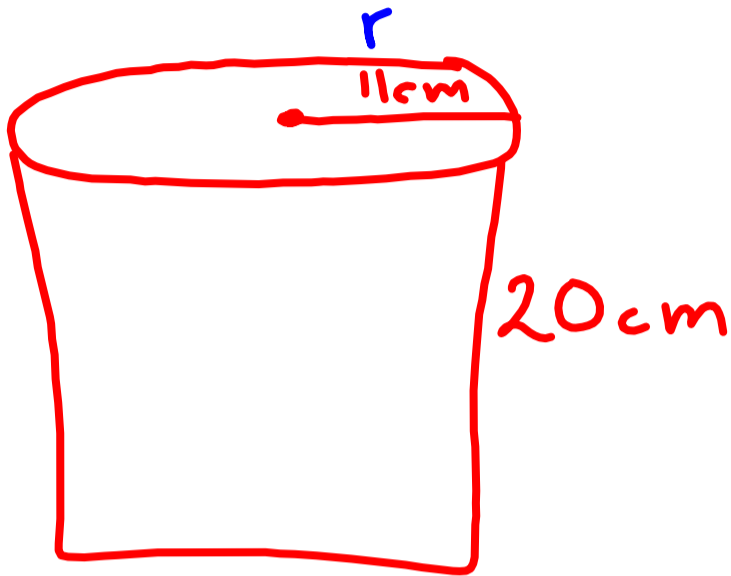
sign
same

2) $(-28) \div (\underline{+4}) = (-7)$

3) $(+60) \div (\underline{-5}) = (-12)$

Division can be written...

$$\frac{(-150)}{(+25)} = (-6)$$



Find Surface Area

$$\begin{aligned}
 SA &= 2\pi r^2 + 2\pi r H \\
 &= (2)(3.14)(11\text{cm})^2 + 2(3.14)(11\text{cm})(20\text{cm}) \\
 &= (2)(3.14)121\text{cm}^2 + 2(3.14)(11\text{cm})(20\text{cm}) \\
 &= 759.88\text{cm}^2 + 1381.6\text{cm}^2 \\
 &= \boxed{2141.48\text{cm}^2}
 \end{aligned}$$

Find Volume

$$\begin{aligned}
 V &= \pi r^2 H \\
 &= (3.14)(11\text{cm})^2 (20\text{cm}) \\
 &= (3.14)(121\text{cm}^2)(20\text{cm}) \\
 &= \boxed{7598.8\text{cm}^3}
 \end{aligned}$$

WS

17 Evaluate.

a) $(+9) \times (+10)$

b) $(+6) \times (-11)$

c) $(+96) \div (-16)$

d) $(+39) \div (+3)$

e) $(-8) \times (+6)$

f) $(-36) \div (+9)$

g) $(-44) \div (-4)$

h) $(-5) \times (-1)$

18) Find the missing term

a) $\quad - (-6) = (-10)$

b) $(+4) \times \quad = (-4)$

c) $(+24) \div \quad = (-6)$

c) $(+4) \times \quad = (+4)$

d) $(+14) \times (-2) = \quad$

$(-15) \times \quad = (+105)$

f) $\quad \div (-10) = (-5)$

g) $(-18) \times (-4)$

h) $(-54) \div \quad = (+9)$

i) $(\quad) \div (-12) = (+96)$

Quiz & Worksheet - Formula for Independent Events in Probability

WS

1. A bag contains 6 red, 2 yellow, and 7 orange marbles. What is the probability of drawing two red marbles out of the bag (with replacement)?

- $2/5$
- $3/5$
- $4/25$
- $1/7$

2. A jar contains 4 yellow, 3 blue, 5 orange, and 8 black balls. What is the probability of reaching into the jar and pulling out a blue and an orange ball (with replacement)?

- $3/80$
- $1/5$
- $3/76$
- None of the answers are correct.

3. What is the probability of the following compound event involving a coin and a standard die?

$P(\text{Heads}, \text{Odd } \#)$

- $3/4$
- $1/2$
- 0
- $1/4$

Create your account to access this entire worksheet

A Premium account gives you access to all lessons, practice exams, quizzes & worksheets



Access to all video lessons



Quizzes, practice exams & worksheets



Access to experts for homework questions

1.



Ricardo has the spinner pictured here and a bag of marbles filled with 2 red marbles, 3 green marbles, and 3 blue marbles. What is the probability that Ricardo spins red on the spinner and picks a red marble out of the bag?

A $1/2$

B $1/8$

C $1/4$

D $1/16$

2. How many outcomes are there with tossing a coin and rolling a dice?

A 2

B 24

C 6

D 12

3.



What is the probability of picking a blue marble, putting it back in the bag, then picking a red marble?

A $\frac{3}{7} \times \frac{3}{7}$

B $\frac{4}{7} \times \frac{3}{6}$

C $\frac{4}{7} \times \frac{3}{7}$

D $\frac{4}{7} \times \frac{4}{7}$

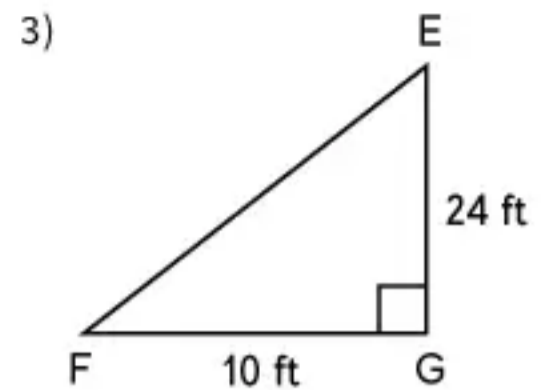
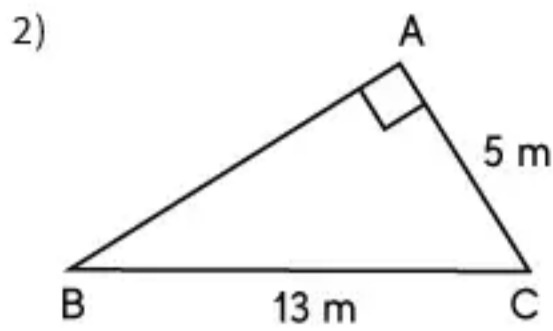
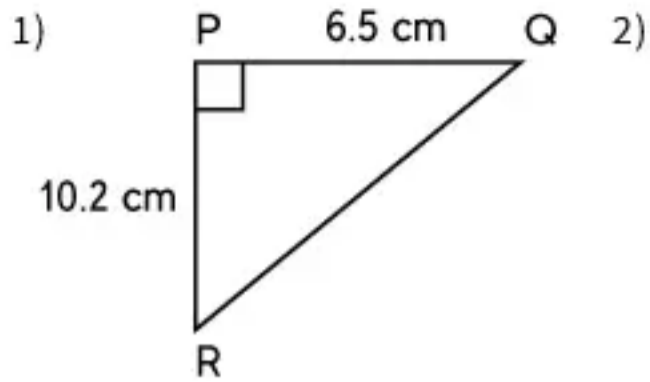
4.



If you spin two times, what is the probability of landing on green both times?

WS Pythagoras' Theorem Worksheet

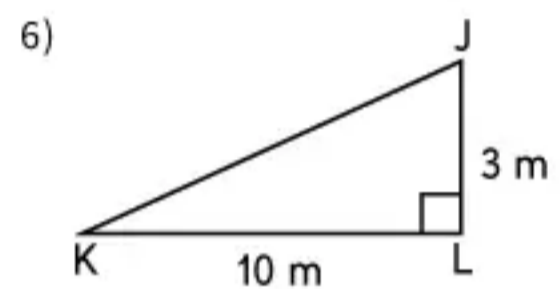
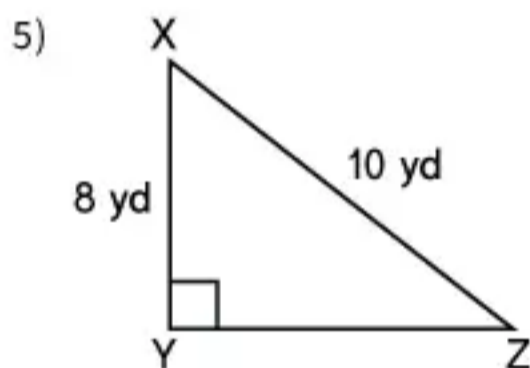
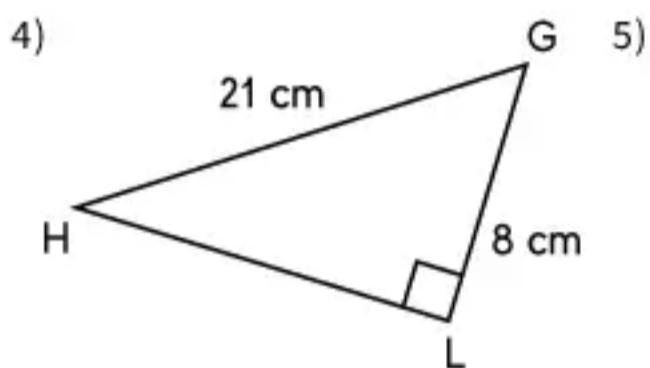
Find the lengths of the unknown sides in the given right triangles.



QR = _____

AB = _____

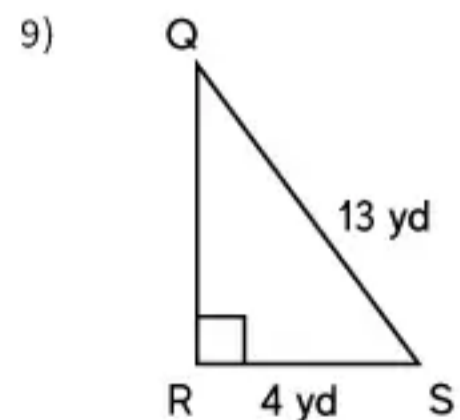
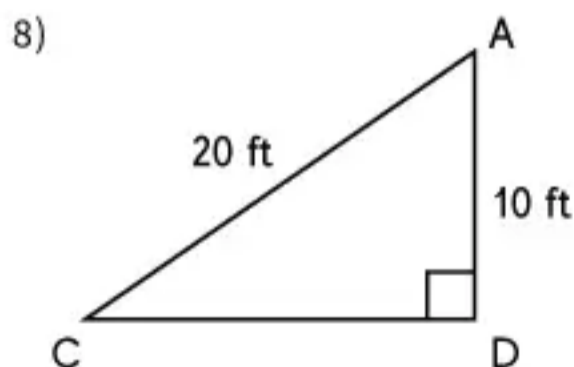
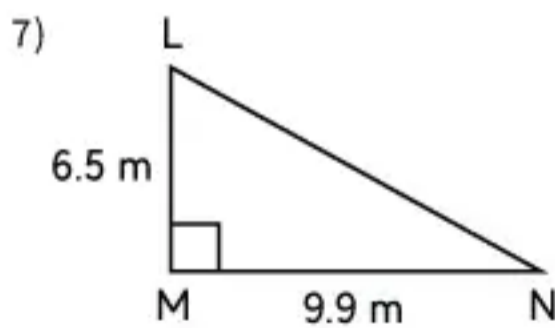
EF = _____



HL = _____

YZ = _____

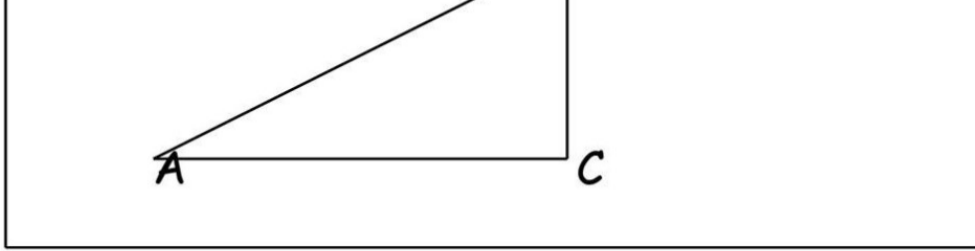
KJ = _____



LN = _____

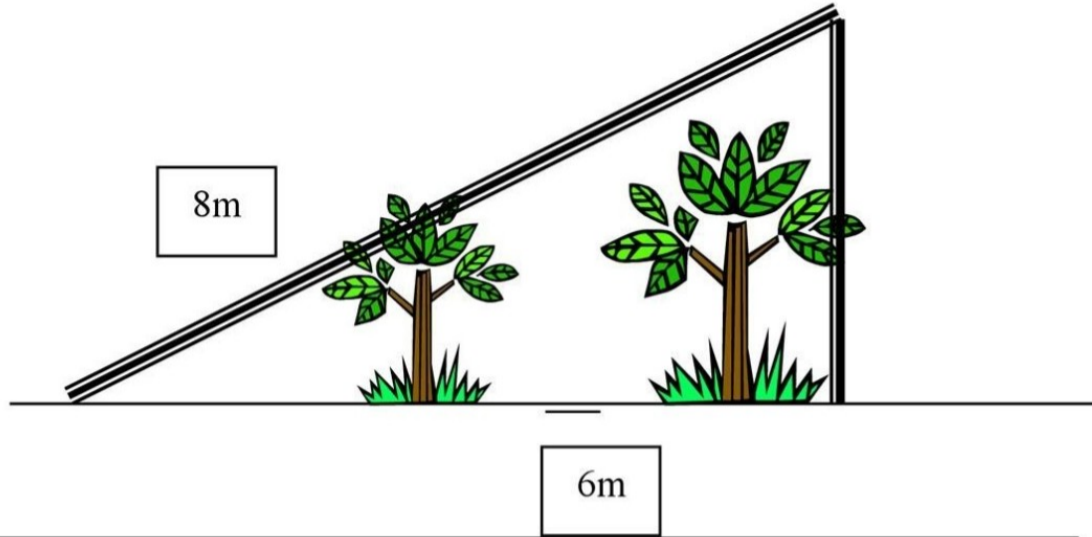
CD = _____

QR = _____



Q3) A ladder of 8 metres long. It leans against a wall with one end on the ground 6 metres from the wall. The other end just reaches a windowsill. Calculate the height of the windowsill above the ground.

WS



Page 1

Determine whether each set of numbers is a Pythagorean triple.

1) 6, 8, 10

2) 16, 7, 3

3) 32, 21, 26

4) 20, 25, 15

WS SOLUTION

17 Evaluate.

a) $(+9) \times (+10) = (+90)$ b) $(+6) \times (-11) = (-66)$ c) $(+96) \div (-16) = (-6)$
d) $(+39) \div (+3) = (+13)$ e) $(-8) \times (+6) = (-48)$ f) $(-36) \div (+9) = (-4)$
g) $(-44) \div (-4) = (+11)$ h) $(-5) \times (-1) = (+5)$

18) Find the missing term

a) $(+60) \div (-6) = (-10)$ b) $(+44) \div (-11) = (-4)$
c) $(+24) \div (-4) = (-6)$ c) $(+48) \div (+12) = (+4)$
d) $(+14) \times (-2) = (-28)$ e) $(-15) \times \underline{\hspace{2cm}} = (+105)$
f) $(+50) \div (-10) = (-5)$ g) $(-18) \times (-4) = (+72)$
h) $(-54) \div (-6) = (+9)$ i) $(\underline{\hspace{2cm}}) \div (-12) = (+96)$
(-1152)

Quiz & Worksheet - Formula for Independent Events in Probability

WS SOLUTION

WS

1. A bag contains 6 red, 2 yellow, and 7 orange marbles. What is the probability of drawing two red marbles out of the bag (with replacement)?

2/5

3/5

4/25

1/7

$$P(\text{Red}) \times P(\text{Red})$$

$$\frac{6}{15} \times \frac{6}{15}$$

$$\frac{2}{5} \times \frac{2}{5}$$

$$\frac{4}{25}$$

2. A jar contains 4 yellow, 3 blue, 5 orange, and 8 black balls. What is the probability of reaching into the jar and pulling out a blue and an orange ball (with replacement)?

3/80

1/5

3/76

None of the answers are correct.

$$P(\text{Blue}) \times P(\text{orange})$$

$$\frac{3}{20} \times \frac{5}{20}$$

$$\frac{15}{400}$$

$$\frac{3}{80}$$

OR

$$\frac{3}{20} \times \frac{5}{20}$$

$$\frac{3}{20} \times \frac{1}{4}$$

$$\frac{3}{80}$$

3. What is the probability of the following compound event involving a coin and a standard die?
P (Heads , Odd #)

3/4

1/2

0

1/4

$$P(\text{Heads}) \times P(\text{odd on Die})$$

$$\frac{1}{2} \times \frac{3}{6}$$

$$\frac{1}{2} \times \frac{1}{2}$$

$$\frac{1}{4}$$

Create your account to access this entire worksheet

A Premium account gives you access to all lessons, practice exams, quizzes & worksheets



Access to all video lessons



Quizzes, practice exams & worksheets

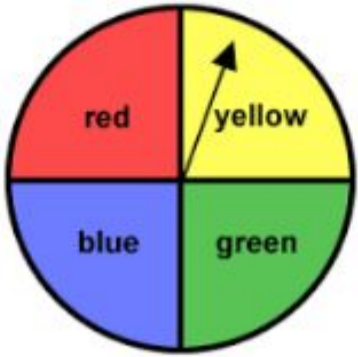


Access to experts for homework questions

WS SOLUTION

WS

1.



Ricardo has the spinner pictured here and a bag of marbles filled with 2 red marbles, 3 green marbles, and 3 blue marbles. What is the probability that Ricardo spins red on the spinner and picks a red marble out of the bag?

$$P(\text{Red spinner}) \times P(\text{Red Marble})$$

$$\frac{1}{4} \times \frac{2}{8} \rightarrow \text{Reduce}$$

$$\frac{1}{4} \times \frac{1}{4} = \frac{1}{16}$$

A 1/2

B 1/8

C 1/4

D 1/16

2. How many outcomes are there with tossing a coin and rolling a dice?

A 2

B 24

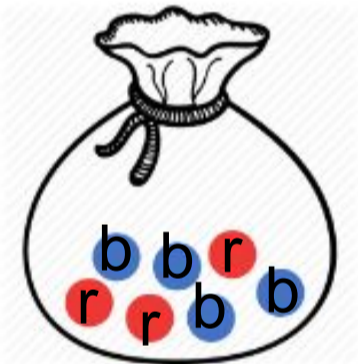
C 6

D 12

Coin \rightarrow 2 outcomes
Die \rightarrow 6 outcomes

$$\text{Total} \Rightarrow 2 \times 6 = 12$$

3.



What is the probability of picking a blue marble, putting it back in the bag, then picking a red marble?

$$P(\text{Blue}) \times P(\text{Red})$$

$$\frac{4}{7} \times \frac{3}{7} = \frac{12}{49}$$

A $\frac{3}{7} \times \frac{3}{7}$

B $\frac{4}{7} \times \frac{3}{6}$

C $\frac{4}{7} \times \frac{3}{7}$

D $\frac{4}{7} \times \frac{4}{7}$

4.



If you spin two times, what is the probability of landing on green both times?

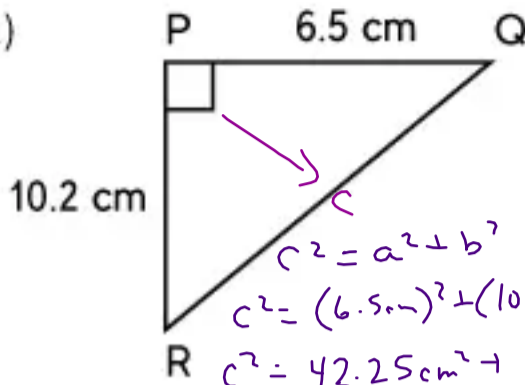
$$P(\text{Green}) \times P(\text{Green})$$

$$\frac{1}{6} \times \frac{1}{6} = \frac{1}{36}$$

Pythagoras' Theorem Worksheet WS SOLUTION

Find the lengths of the unknown sides in the given right triangles.

1) 2) 3)



$$c^2 = a^2 + b^2$$

$$c^2 = (6.5\text{m})^2 + (10.2\text{m})^2$$

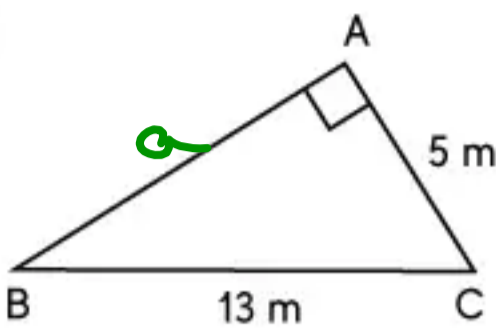
$$c^2 = 42.25\text{cm}^2 + 104.04\text{cm}^2$$

$$c^2 = 146.29\text{cm}^2$$

$$\sqrt{c^2} = \sqrt{146.29\text{cm}^2}$$

$$c \approx 12.1\text{cm}$$

QR = 12.1cm



$$a^2 = c^2 - b^2$$

$$a^2 = (13\text{m})^2 - (5\text{m})^2$$

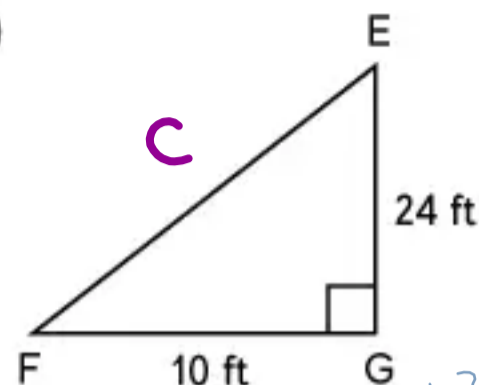
$$a^2 = 169\text{m}^2 - 25\text{m}^2$$

$$a^2 = 144\text{m}^2$$

$$\sqrt{a^2} = \sqrt{144\text{m}^2}$$

$$a = 12\text{m}$$

AB = 12m



$$c^2 = a^2 + b^2$$

$$c^2 = (10\text{ft})^2 + (24\text{ft})^2$$

$$c^2 = 100\text{ft}^2 + 576\text{ft}^2$$

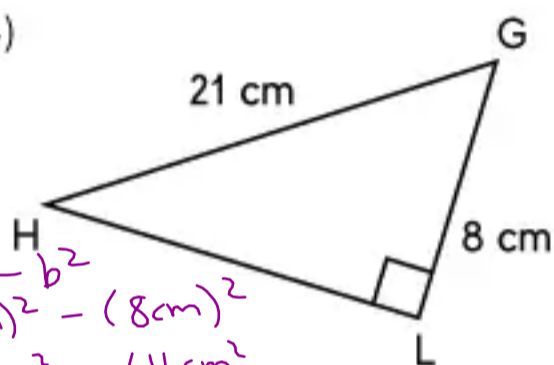
$$c^2 = 676\text{ft}^2$$

$$\sqrt{c^2} = \sqrt{676\text{ft}^2}$$

$$c = 26\text{ft}$$

EF = C = 26ft

4) 5) 6)



$$a^2 = c^2 - b^2$$

$$a^2 = (21\text{cm})^2 - (8\text{cm})^2$$

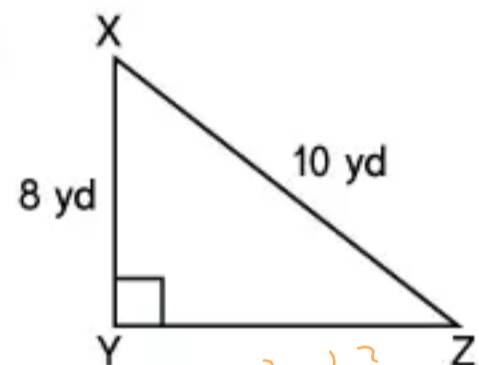
$$a^2 = 441\text{cm}^2 - 64\text{cm}^2$$

$$a^2 = 377\text{cm}^2$$

$$\sqrt{a^2} = \sqrt{377\text{cm}^2}$$

$$a \approx 19.4\text{cm}$$

HL = 19.4cm



$$a^2 = c^2 - b^2$$

$$a^2 = (10\text{yd})^2 - (8\text{yd})^2$$

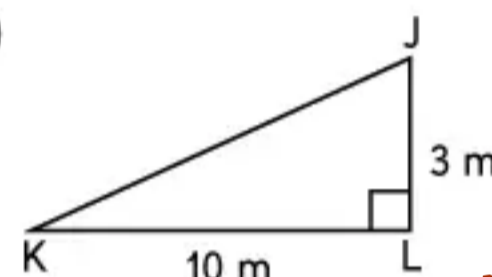
$$a^2 = 100\text{yd}^2 - 64\text{yd}^2$$

$$a^2 = 36\text{yd}^2$$

$$\sqrt{a^2} = \sqrt{36\text{yd}^2}$$

$$a = 6\text{yd}$$

YZ = 6yd



$$c^2 = a^2 + b^2$$

$$c^2 = (10\text{m})^2 + (3\text{m})^2$$

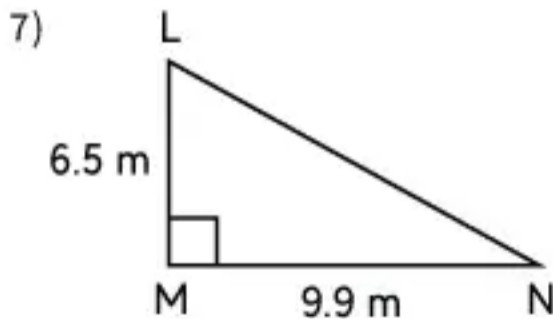
$$c^2 = 100\text{m}^2 + 9\text{m}^2$$

$$c^2 = 109\text{m}^2$$

$$\sqrt{c^2} = \sqrt{109\text{m}^2}$$

$$c = 10.4\text{m}$$

KJ = 10.4m



$$c^2 = a^2 + b^2$$

$$c^2 = (6.5\text{m})^2 + (9.9\text{m})^2$$

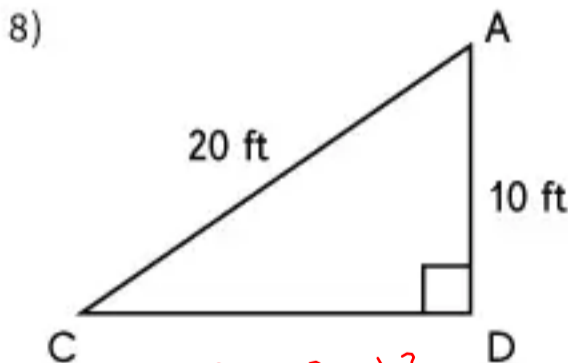
$$c^2 = 42.25\text{m}^2 + 98.01\text{m}^2$$

$$c^2 = 140.26\text{m}^2$$

$$\sqrt{c^2} = \sqrt{140.26\text{m}^2}$$

$$c \Rightarrow$$

LN = 11.8m



$$a^2 = c^2 - b^2$$

$$a^2 = (20\text{ft})^2 - (10\text{ft})^2$$

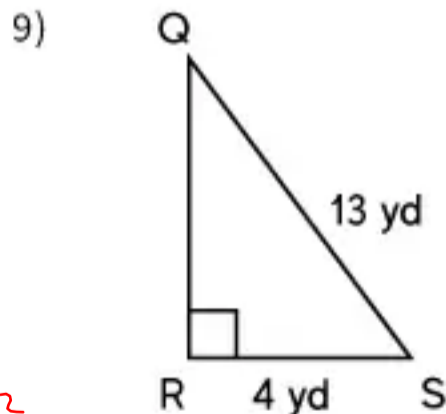
$$a^2 = 400\text{ft}^2 - 100\text{ft}^2$$

$$a^2 = 300\text{ft}^2$$

$$\sqrt{a^2} = \sqrt{300\text{ft}^2}$$

$$a \Rightarrow$$

CD = 17.3ft



$$a^2 = c^2 - b^2$$

$$a^2 = (13\text{yd})^2 - (4\text{yd})^2$$

$$a^2 = 169\text{yd}^2 - 16\text{yd}^2$$

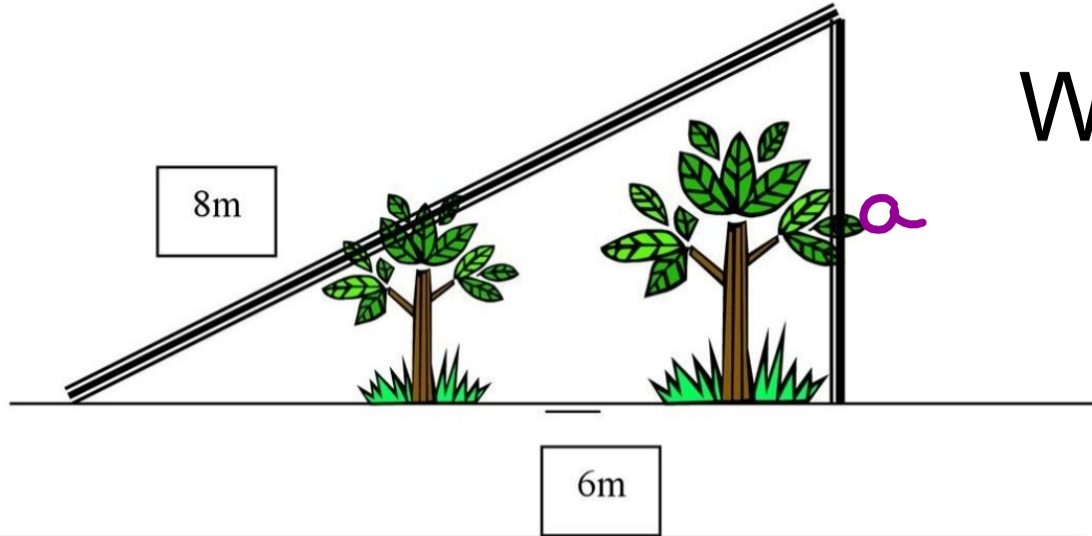
$$a^2 = 153\text{yd}^2$$

$$a = \sqrt{153\text{yd}^2}$$

$$a \Rightarrow$$

QR = 12.4 yd

Q3) A ladder of 8 metres long. It leans against a wall with one end on the ground 6 metre from the wall. The other end just reaches a windowsill. Calculate the height of the windowsill above the ground.



Page 1

WS SOLUTION

$$a^2 = c^2 - b^2$$

$$a^2 = (8\text{m})^2 - (6\text{m})^2$$

$$a^2 = 64\text{m}^2 - 36\text{m}^2$$

$$a^2 = 28\text{m}^2$$

$$\sqrt{a^2} = \sqrt{28\text{m}^2}$$

$$a \approx 5.3\text{m}$$

Determine whether each set of numbers is a Pythagorean triple.

1) 6, 8, 10

$$\begin{array}{l} \downarrow \quad \downarrow \\ 6^2 + 8^2 \\ 36 + 64 \\ 100 \end{array} \quad \left. \begin{array}{l} \\ \\ \\ \end{array} \right\} \begin{array}{l} 10^2 \\ 100 \end{array}$$

same
Yes

2) 16, 7, 3

$$\begin{array}{l} 16^2 \\ 256 \end{array} \quad \left. \begin{array}{l} \\ \\ \\ \end{array} \right\} \begin{array}{l} 7^2 + 3^2 \\ 49 + 9 \\ 58 \end{array}$$

Not same
Not a triple

3) 32, 21, 26

$$\begin{array}{l} 32^2 \\ 1024 \end{array} \quad \left. \begin{array}{l} \\ \\ \\ \end{array} \right\} \begin{array}{l} 21^2 + 26^2 \\ 441 + 676 \\ 1117 \end{array}$$

Not same
Not a triple

4) 20, 25, 15

$$\begin{array}{l} 25^2 \\ 625 \end{array} \quad \left. \begin{array}{l} \\ \\ \\ \end{array} \right\} \begin{array}{l} 20^2 + 15^2 \\ 400 + 225 \\ 625 \end{array}$$

Same
So yes a triple