



## Warm Up Grade 8

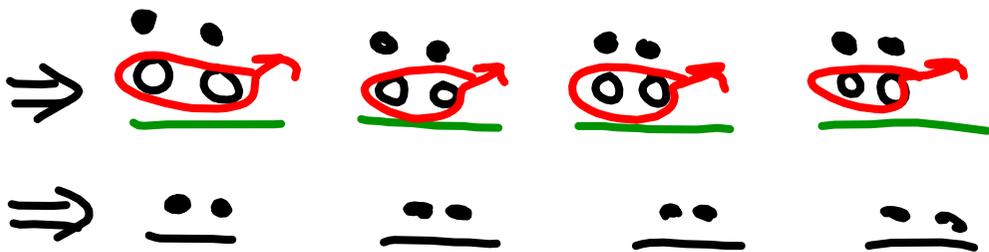


$$\bigcirc = -$$

$$\bullet = +$$

1) Use tile to model the product of  $(-4) \times (-2) = (+8)$

Remove 4 groups of 2 unshaded



2) Find the product using the distributive property **Box Method**

a)  $(-21) \times (+46) = (-966)$

b)  $(-40) \times (-34) = (+1360)$

	20	1
40	800	40
6	120	6

$$\begin{array}{r} 800 \\ 120 \\ 40 \\ + 6 \\ \hline 966 \end{array}$$

	30	4
40	1200	160

$$\begin{array}{r} 1200 \\ + 160 \\ \hline 1360 \end{array}$$

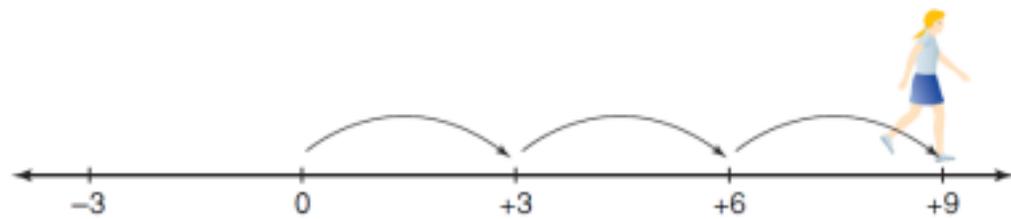
## Second number + is facing destination

Divide:  $(+9) \div (+3)$  - Not facing destination

We need to find how many steps of  $+3$  make  $+9$ .

The step size,  $+3$ , is positive; so, walk forward.

Start at 0. Take steps forward to end up at  $+9$ .



We took 3 steps. We are facing the positive end of the line.

So,  $(+9) \div (+3) = +3$

$$(?) \times (+3) = (+9)$$

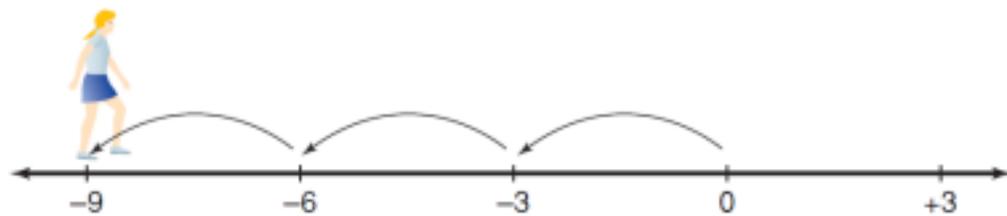
$$\begin{array}{c} \uparrow \\ (+3) \end{array}$$

Divide:  $(-9) \div (-3)$

We need to find how many steps of  $-3$  make  $-9$ .

The step size,  $-3$ , is negative; so, walk backward.

Start at 0. Take steps backward to end up at  $-9$ .



We took 3 steps. We are facing the positive end of the line.

So,  $(-9) \div (-3) = +3$

$$(?) \times (-3) = (-9)$$

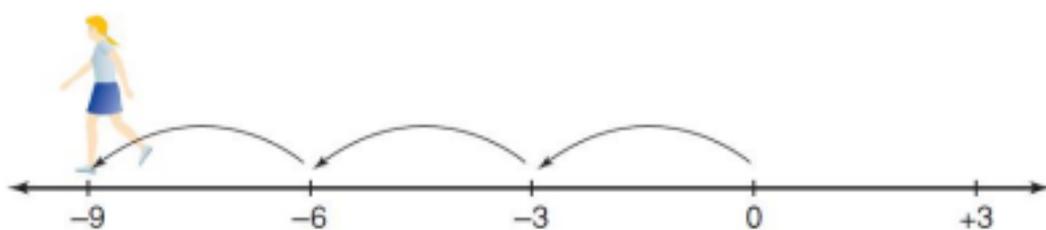
$$(-9) \div (-3) = (+3)$$

Divide:  $(-9) \div (+3)$

We need to find how many steps of  $+3$  take us to  $-9$ .

The step size,  $+3$ , is positive; so, walk forward.

Start at 0. To end up at  $-9$ , we took 3 steps forward.



We are facing the negative end of the line.

So,  $(-9) \div (+3) = -3$

$$(?) \times (+3) = (-9)$$



## Recall Modeling Integer Multiplication

### Using Number Lines

$$(+)\times(-)=(-)$$

$$(-)\times(+)=(-)$$

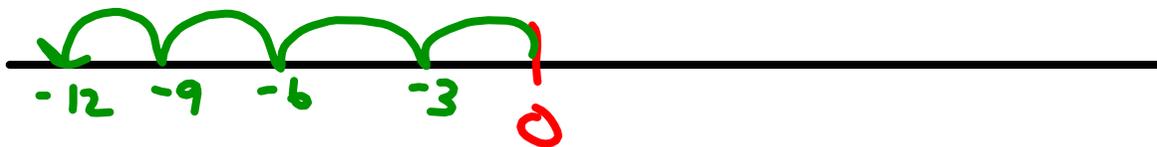
$$(+)\times(+)$$

(Arrow size) X (# of jumps <sup>Always +</sup> or arrows) = (STOP)

Due to the commutative law you can change the order of multiplication

Ex) Model  $(-3)\times(+4) = (+4)\times(-3)$

4 jumps of -3





## Modeling Integer Division

### Using Number Lines



$$(\text{STOP}) \div (\# \text{ of jumps or arrows}) = (\text{Arrow size})$$

OR

$$(\text{STOP}) \div (\text{Arrow size}) = (\# \text{ of jumps or arrows})$$

$$(+ ) \times (- ) = (- )$$

$$(- ) \times (+ ) = (- )$$

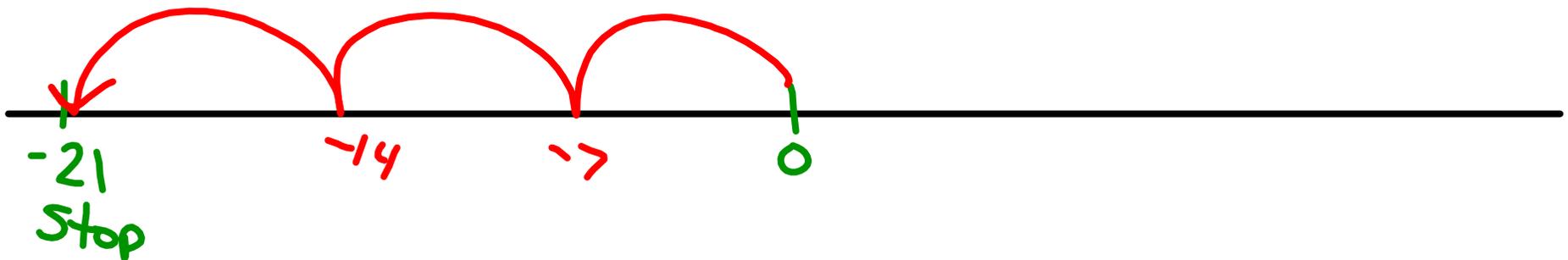
$$(+ ) \times (+ ) = (+ )$$

Diff  $\Rightarrow$  -

Same  $\Rightarrow$  +

Model the following with a number line

$$(-21) \div (+3) = -7$$



## Dividing Integers

↗ reverse of multiplication

$(+7) \times (+4) = (+28)$  so we also know that  $(+28) \div (+7) = (+4)$

$$(+28) \div (+4) = (+7)$$

$(+5) \times (-8) = (-40)$  so we also know that  $(-40) \div (-8) = (+5)$

and  $(-40) \div (+5) = (-8)$

$$\div$$

$(-9) \times (+3) = (-27)$  so we also know that  $(-27) \div (+3) = (-9)$

and  $(-27) \div (-9) = (+3)$

$$\div$$

$(-6) \times (-2) = (+12)$  so we also know that  $(+12) \div (-6) = (-2)$

and  $(+12) \div (-2) = (-6)$

$$\div$$

From the above information, what can you determine about

(a) a positive divided by a positive?

the answer will always be positive

$$(+)\div(+)=(+)$$

(b) a positive divided by a negative?

The answer will always be negative

$$(+)\div(-)=(-)$$

(c) a negative divided by a positive?

The answer will always be negative

$$(-)\div(+)=(-)$$

(d) a negative divided by a negative?

The answer will always be positive.

$$(-)\div(-)=(+)$$

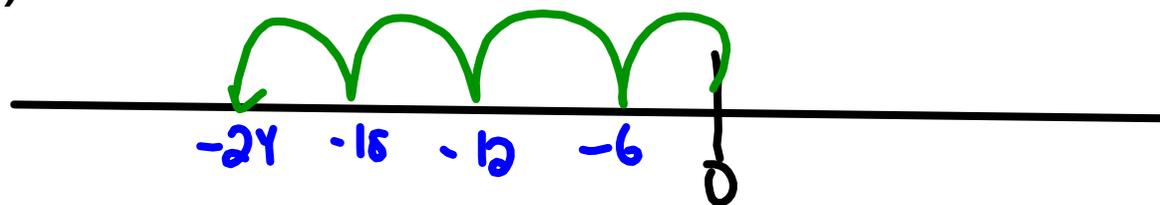
**Quotient** is the number that results from the division of one number by another.

$$24 \div 3 = 8$$

← quotient

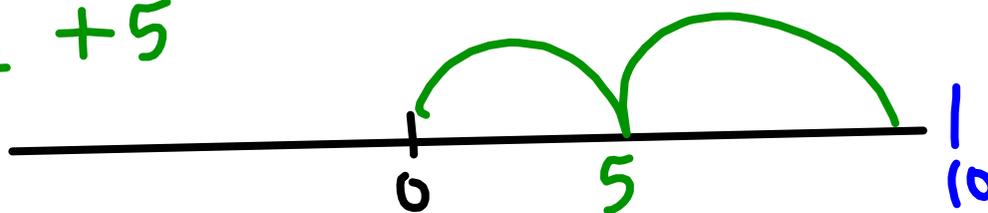
# Rethink to multiplying if struggling

*Stop*  
*#arrows*  
 $(-24) \div (+4) = (-6)$



Then Draw number line

b)  $(+10) \div (+2) = +5$



Divide the following using rules:

a)  $(-72) \div (+8)$

$(-9)$

b)  $(-45) \div (-9)$

$(+5)$

c)  $(+24) \div (+2)$

$(+12)$

# Class/Homework

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#3(a,d)

#4(a,b,c)

#5

#6(a,b,c,d)

#7a(i), b(i) } NO MODELLING

#8(abcde) } Just Use Rules

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#9, #11, #13, #18

3. Write a related multiplication equation for each division equation.

ex)  $(-12) \div (+2) = (-6)$   $\rightarrow$   $(-6) \times (+2) = (-12)$   
 $(+2) \times (-6) = (-12)$

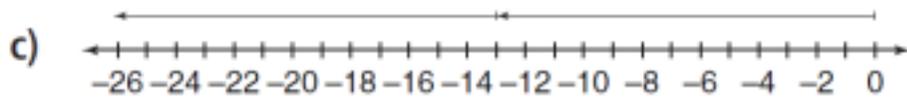
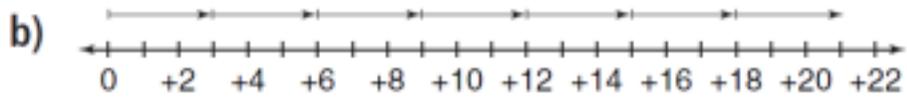
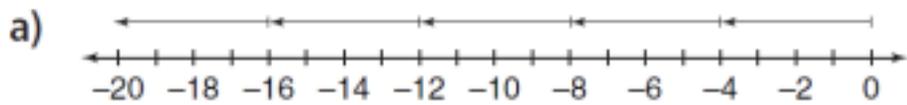
a)  $(+25) \div (+5) = +5$     b)  $(+24) \div (-2) = -12$     c)  $(-14) \div (-7) = +2$     d)  $(-18) \div (+6) = -3$

$(\text{STOP}) \div (\text{Arrow size}) = (\# \text{ of jumps or arrows})$  <sup>Always +</sup>

OR

$(\text{STOP}) \div (\# \text{ of jumps or arrows}) = (\text{Arrow size})$  <sup>Always +</sup>

4. Which integer division does each number line represent? Find each quotient.



$$(\text{STOP}) \div (\# \text{ of jumps or arrows}) = (\text{Arrow size})$$

$$\text{OR } (\text{STOP}) \div (\text{Arrow size}) = (\# \text{ of jumps or arrows})$$

- 5.** Enrico walked a number line to model a division. He started at 0. Enrico took steps forward of size 4. He ended up at  $-24$ . Which division did Enrico model? How did you find out?



- 6.** Use a number line. Find each quotient.

**a)**  $(+8) \div (+1)$       **b)**  $(-6) \div (-2)$

**c)**  $(-16) \div (+8)$       **d)**  $(-3) \div (-1)$

**e)**  $(+15) \div (-3)$       **f)**  $(-20) \div (+2)$

Write a division statement for the following and answer

7. a) How many sets?      Ex) 10 yellow grouped in sets of 2  $\rightarrow (+10) \div (+2) = (+5)$
- i) 12 yellow tiles grouped in sets of 6
  - ii) 15 red tiles grouped in sets of 3
- b) How many in each set?
- i) 8 yellow tiles shared among 2 sets
  - iii) 21 red tiles shared among 7 sets

8. Use Rules to find the Quotient (No Modeling)

a)  $(+18) \div (+6)$     b)  $(-18) \div (+9)$     c)  $(-16) \div (-4)$     d)  $(+21) \div (-7)$     e)  $(+15) \div (-5)$     f)  $(-16) \div (-8)$

9. Use Rules to find the Quotient (No Modeling)

a)  $(+8) \div (+4)$     b)  $(-8) \div (-4)$     c)  $(+8) \div (-4)$     d)  $(-8) \div (+4)$

Write a division equation for each word problem

- 11.** The temperature rose  $3^{\circ}\text{C}$  each hour for a total change of  $+12^{\circ}\text{C}$ . Use integers to find the number of hours the change in temperature took.
- 13.** A submarine was at the surface of the ocean. It made 4 identical plunges in a row. Its final depth was 148 m below sea level. What was the depth of each plunge? \_\_\_\_\_

Show your thinking

- 18. Take It Further** Reena deposits \$4 into her savings account each week. Today, Reena's account has a balance of \$16.
- a) How many weeks from now will Reena's account have a balance of \$40?
- b) What was the balance in Reena's account 2 weeks ago?

Explain how you can use integers to model each situation.